Angles and Fractional Parts of a Circle

Find how many \( \frac{1}{6} \) turns make a complete circle.

Materials: fraction circles

**Step 1** Place a \( \frac{1}{6} \) piece so the tip of the fraction piece is on the center of the circle. Trace the fraction piece by drawing along the dashed lines in the circle.

**Step 2** Shade and label the angle formed by the \( \frac{1}{6} \) piece.

**Step 3** Place the \( \frac{1}{6} \) piece on the shaded angle. Turn it clockwise (in the direction that the hands on a clock move). Turn the fraction piece to line up directly beside the shaded section.

**Step 4** Trace the fraction piece. Shade and label it. You have traced 2 sixths in all.

**Step 5** Repeat until you have shaded the entire circle.

There are six angles that come together in the center of the circle.

So, you need six \( \frac{1}{6} \) turns to make a circle.

Tell what fraction of the circle the shaded angle represents.

1. [Diagram]
2. [Diagram]
3. [Diagram]
Degrees

Angles are measured in units called degrees. The symbol for degrees is °. If a circle is divided into 360 equal parts, then an angle that turns through 1 part of the 360 measures 1°.

An angle that turns through \( \frac{50}{360} \) of a circle measures 50°.

**Find the measure of an angle that turns through \( \frac{1}{6} \) of a circle.**

**Step 1** Find a fraction that is equivalent to \( \frac{1}{6} \) with 360 in the denominator. Think: \( 6 \times 60 = 360 \).

\[
\frac{1}{6} = \frac{1 \times 60}{6 \times 60} = \frac{60}{360}
\]

**Step 2** Look at the numerator of \( \frac{60}{360} \).

The numerator tells how many degrees are in \( \frac{1}{6} \) of a circle.

So, an angle that turns through \( \frac{1}{6} \) of a circle measures 60°.

**Tell the measure of the angle in degrees.**

1. 
   - \( \frac{39}{360} \)

2. 
   - \( \frac{1}{5} \)

3. 
   - \( \frac{1}{8} \)

4. 
   - \( \frac{5}{12} \)
Measure and Draw Angles

A protractor is a tool for measuring the size of an angle.

Follow the steps below to measure $\angle ABC$.

**Step 1** Place the center point of the protractor on vertex $B$ of the angle.

**Step 2** Align the 0° mark on the protractor with ray $BC$. Note that the 0° mark is on the outer scale or top scale.

**Step 3** Find where ray $BA$ intersects the same scale.

**Step 4** Read the angle measure on the scale.

The $m\angle ABC = 30^\circ$.

Use a protractor to find the angle measure.

1. $m\angle FGH$ 
2. $m\angle KMN$

Use a protractor to draw the angle.

3. 110°
4. 55°
Join and Separate Angles

The measure of an angle equals the sum of the measures of its parts.

Use your protractor and the angles at the right.

Step 1 Measure $\angle ABC$ and $\angle CBD$. Record the measures.

$m\angle ABC = 35^\circ$; $m\angle CBD = 40^\circ$

Step 2 Find the sum of the measures.

$35^\circ + 40^\circ = 75^\circ$

Step 3 Measure $\angle ABD$. Record the measure.

$m\angle ABD = 75^\circ$

So, $m\angle ABC + m\angle CBD = m\angle ABD$.

Add to find the measure of the angle. Write an equation to record your work.

1. $m\angle EGH = \_\_\_$

2. $m\angle KLN = \_\_\_$

3. $m\angle PRT = \_\_\_$

Use a protractor and the art at the right.

4. Find the measure of each angle. Label each angle with its measure.

5. Write the sum of the angle measures as an equation.
Problem Solving • Unknown Angle Measures

Use the strategy draw a diagram.

Mrs. Allen is cutting a piece of wood for a set for the school play. She needs a piece of wood with a 60° angle. After the cut, what is the angle measure of the part left over?

Read the Problem

<table>
<thead>
<tr>
<th>What do I need to find?</th>
<th>What information do I need to use?</th>
<th>How will I use the information?</th>
</tr>
</thead>
<tbody>
<tr>
<td>I need to find the angle measure of the part left over, or ( \angle PNR ).</td>
<td>I can use the angle measures I know: ( \angle MNP = 60° ) and ( \angle MNR = 110° ).</td>
<td>I can draw a bar model to find the unknown angle measure, or ( \angle PNR ).</td>
</tr>
</tbody>
</table>

Solve the Problem

I can draw a bar model to represent the problem.

Then I can write an equation to solve the problem.

\[
60° + x = 110°
\]

\[
x = 110° - 60°, \text{ or } 50°
\]

So, \( \angle PNR = 50° \).

The angle measure of the part left over is \( 50° \).

1. Cal is cutting a rectangular board as shown. What is the angle measure of the part left over? ______

2. What equation did you use to solve?

[Diagram of a rectangular board with angles labeled 45° and 110°]